CS230: Lecture 3
Attacking Networks with Adversarial Examples
- Generative Adversarial Networks
Kian Katanforoosh
I. Attacking NNs with Adversarial Examples
II. Generative Adversarial Networks
I. Adversarial examples

Discovery (2013): several machine learning models, including state-of-the-art neural networks, are vulnerable to adversarial examples

A. Attacking a network with adversarial examples

B. Defenses against adversarial examples

C. Why are neural networks vulnerable to adversarial examples?
I. A. Attacking a network with adversarial examples

**Goal:** Given a network pretrained on ImageNet, find an input image that will be classified as an iguana.

1. **Rephrasing what we want:**
   Find \( x \) such that: 
   \[
   \hat{y}(x) = y_{\text{iguana}} = \begin{pmatrix}
   0 \\
   1 \\
   \vdots \\
   0 \\
   \end{pmatrix}
   \]

2. **Defining the loss function**
   \[
   L(\hat{y}, y) = \frac{1}{2} \left\| \hat{y}(W, b, x) - y_{\text{iguana}} \right\|^2
   \]

3. **Optimize the image**
   After many iterations
   \[
   x = x - \alpha \frac{\partial L}{\partial x}
   \]

[Ian J. Goodfellow, Jonathon Shlens & Christian Szegedy (2015): Explaining and harnessing adversarial examples]
I. A. Attacking a network with adversarial examples

**Question:** Will the forged image $x$ look like an **iguana**?

Space of possible input images

$256^{32 \times 32 \times 3} \approx 10^{7400}$

Space of real images

Space of images classified as iguanas
**I. A. Attacking a network with adversarial examples**

**Goal:** Given a network pretrained on ImageNet, find an input image displaying a cat but classified as an iguana.

![Image of a cat](image.png)

**Neural network** (pretrained on ImageNet)

---

1. **Rephrasing what we want:**
   
   Find $x$ such that: $\hat{y}(x) = y_{\text{iguana}} = \begin{pmatrix} 0 \\ 1 \\ \vdots \\ 0 \\ 0 \\ \vdots \\ 0 \end{pmatrix}$
   
   And: $x = x_{\text{cat}}$

2. **Defining the loss function**
   
   $L(\hat{y}, y) = \frac{1}{2} \| \hat{y}(W, b, x) - y_{\text{iguana}} \|^2 + \lambda \| x - x_{\text{cat}} \|^2$

3. **Optimize the image**
   
   After many iterations

$$x = x - \alpha \frac{\partial L}{\partial x}$$

---

[Ian J. Goodfellow, Jonathon Shlens & Christian Szegedy (2015): Explaining and harnessing adversarial examples]

Kian Katanforoosh
I. A. Attacking a network with adversarial examples

92% Cat

94% Iguana
I. A. Attacking a network with adversarial examples

\[ 256^{32 \times 32 \times 3} \approx 10^{7400} \]

Space of possible input images

Space of images classified as iguanas

Space of real images

Space of images that look real to humans
Adversarial Examples In The Physical World

[Alexey Kurakin, Ian J. Goodfellow, Samy Bengio (2017): Adversarial examples in the physical world]
Knowledge of the attacker:

- White-box
- Black-box

**Solution 1**
- Create a SafetyNet

**Solution 2**
- Train on correctly labelled adversarial examples

**Solution 3**
- Adversarial training $L_{new} = L(W, b, x, y) + \lambda L(W, b, x_{adv}, y)$

- $x = $ [Image]
- $y = \text{cat}$

[Lu et al. (2017): SafetyNet: Detecting and Rejecting Adversarial Examples Robustly]
[Harini Kannan et al. (2018): Adversarial Logit Pairing]
I. C. Why are neural networks vulnerable to adversarial examples?

Get your pencils ready, we’re switching to iPad.

Do neural networks actually understand the data?

[Yuan et al. (2017): Adversarial Examples: Attacks and Defenses for Deep Learning]
II. Generative Adversarial Networks (GANs)

A. Motivation

B. G/D Game

C. Training GANs

D. Nice results

E. In terms of code

[Ian J. Goodfellow, Jonathon Shlens & Christian Szegedy (2015): Explaining and harnessing adversarial examples]
**Motivation:**
- Data synthesis
- Compress and reconstruct data.
- Find a mapping between spaces.
- Image in-painting

**Approach:** Collect a lot of data, use it to train a model to generate similar data from scratch.

**Intuition:** number of parameters of the model $\ll$ amount of data
II.A - Motivation

**Probability distributions:**

Samples from the “real data distribution”

Samples from the “generated distribution”

[Han Zhang, Tao Xu, Hongsheng Li, Shaoting Zhang, Xiaogang Wang, Xiaolei Huang, Dimitris Metaxas (2017): StackGAN: Text to Photo-realistic Image Synthesis with Stacked Generative Adversarial Networks]
II. Generative Adversarial Networks (GANs)

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[Ian J. Goodfellow, Jonathon Shlens & Christian Szegedy (2015): Explaining and harnessing adversarial examples]
How can we train G to generate images from the true data distributions?

[Han Zhang, Tao Xu, Hongsheng Li, Xiaogang Wang, Xiaolei Huang, Dimitris Metaxas (2017): StackGAN: Text to Photo-realistic Image Synthesis with Stacked Generative Adversarial Networks]
II.B - G/D Game

Run Gradient Descent simultaneously on two minibatches (true data / generated data)

\[
\begin{cases}
 y = 0 & \text{if } x = G(z) \\
 y = 1 & \text{otherwise}
\end{cases}
\]
II.B - G/D Game

End goal: G is outputting images that are indistinguishable from real images for D

$y = 0 \text{ if } x = G(z)$

$y = 1 \text{ otherwise}$
II.B - G/D Game

Training procedure, we want to minimize:

• The cost of the discriminator

\[
J^{(D)} = -\frac{1}{m_{\text{real}}} \sum_{i=1}^{m_{\text{real}}} y_{\text{real}}^{(i)} \cdot \log(D(x^{(i)})) - \frac{1}{m_{\text{gen}}} \sum_{i=1}^{m_{\text{gen}}} (1 - y_{\text{gen}}^{(i)}) \cdot \log(1 - D(G(z^{(i)})))
\]

cross-entropy 1: "D should correctly label real data as 1"

cross-entropy 2: "D should correctly label generated data as 0"

• The cost of the generator

\[
J^{(G)} = -J^{(D)} = \frac{1}{m_{\text{gen}}} \sum_{i=1}^{m_{\text{gen}}} \log(1 - D(G(z^{(i)})))
\]

"G should try to fool D: by minimizing the opposite of what D is trying to minimize"

Labels: \[
\begin{align*}
  y_{\text{real}} & \text{ is always 1} \\
  y_{\text{gen}} & \text{ is always 0}
\end{align*}
\]
II. Generative Adversarial Networks (GANs)

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[Ian J. Goodfellow, Jonathon Shlens & Christian Szegedy (2015): Explaining and harnessing adversarial examples]
II.C - Training GANs

Saturating cost for the generator:

\[
\min \left[ \frac{1}{m_{\text{gen}}} \sum_{i=1}^{m_{\text{gen}}} \log(1 - D(G(z^{(i)}))) \right] \iff \max \left[ \frac{1}{m_{\text{gen}}} \sum_{i=1}^{m_{\text{gen}}} \log(D(G(z^{(i)}))) \right] \iff \min \left[ -\frac{1}{m_{\text{gen}}} \sum_{i=1}^{m_{\text{gen}}} \log(D(G(z^{(i)}))) \right]
\]

Non-saturating cost:

\[
J^{(G)} = -\frac{1}{m_{\text{gen}}} \sum_{i=1}^{m_{\text{gen}}} \log(D(G(z^{(i)})))
\]

Saturating cost:

\[
J^{(G)} = \frac{1}{m_{\text{gen}}} \sum_{i=1}^{m_{\text{gen}}} \log(1 - D(G(z^{(i)})))
\]

[Ian Goodfellow (2014): NIPS Tutorial: GANs]
Note that:

\[
\min \left[ \frac{1}{m_{\text{gen}}} \sum_{i=1}^{m_{\text{gen}}} \log(1 - D(G(z^{(i)}))) \right] \iff \max \left[ \frac{1}{m_{\text{gen}}} \sum_{i=1}^{m_{\text{gen}}} \log(D(G(z^{(i)}))) \right] \iff \min \left[ -\frac{1}{m_{\text{gen}}} \sum_{i=1}^{m_{\text{gen}}} \log(D(G(z^{(i)}))) \right]
\]

New training procedure, we want to minimize:

\[
J^{(D)} = -\frac{1}{m_{\text{real}}} \sum_{i=1}^{m_{\text{real}}} y^{(i)}_{\text{real}} \cdot \log(D(x^{(i)})) - \frac{1}{m_{\text{gen}}} \sum_{i=1}^{m_{\text{gen}}} (1 - y^{(i)}_{\text{gen}}) \cdot \log(1 - D(G(z^{(i)})))
\]

\(\text{cross-entropy 1:}\)

"D should correctly label real data as 1"

\(\text{cross-entropy 2:}\)

"D should correctly label generated data as 0"

\[
J^{(G)} = -\frac{1}{m_{\text{gen}}} \sum_{i=1}^{m_{\text{gen}}} \log(D(G(z^{(i)})))
\]

"G should try to fool D: by minimizing this"
Table 1: Generator and discriminator loss functions. The main difference whether the discriminator outputs a probability (MM GAN, NS GAN, DRAGAN) or its output is unbounded (WGAN, WGAN GP, LS GAN, BEGAN), whether the gradient penalty is present (WGAN GP, DRAGAN) and where is it evaluated. We chose those models based on their popularity.

<table>
<thead>
<tr>
<th>GAN</th>
<th>Discriminator Loss</th>
<th>Generator Loss</th>
</tr>
</thead>
<tbody>
<tr>
<td>MM GAN</td>
<td>( \mathcal{L}<em>D^{GAN} = -\mathbb{E}</em>{x \sim p_d}[\log(D(x))] - \mathbb{E}_{\hat{x} \sim p_g}[\log(1 - D(\hat{x}))] )</td>
<td>( \mathcal{L}<em>G^{GAN} = \mathbb{E}</em>{\hat{x} \sim p_g}[\log(1 - D(\hat{x}))] )</td>
</tr>
<tr>
<td>NS GAN</td>
<td>( \mathcal{L}<em>D^{NSGAN} = -\mathbb{E}</em>{x \sim p_d}[\log(D(x))] - \mathbb{E}_{\hat{x} \sim p_g}[\log(1 - D(\hat{x}))] )</td>
<td>( \mathcal{L}<em>G^{NSGAN} = -\mathbb{E}</em>{\hat{x} \sim p_g}[\log(D(\hat{x}))] )</td>
</tr>
<tr>
<td>WGAN</td>
<td>( \mathcal{L}<em>D^{WGAN} = -\mathbb{E}</em>{x \sim p_d}[D(x)] + \mathbb{E}_{\hat{x} \sim p_g}[D(\hat{x})] )</td>
<td>( \mathcal{L}<em>G^{WGAN} = -\mathbb{E}</em>{\hat{x} \sim p_g}[D(\hat{x})] )</td>
</tr>
<tr>
<td>WGAN GP</td>
<td>( \mathcal{L}_D^{WGANGP} = \mathcal{L}<em>D^{WGAN} + \lambda \mathbb{E}</em>{\hat{x} \sim p_g}[(</td>
<td></td>
</tr>
<tr>
<td>LS GAN</td>
<td>( \mathcal{L}<em>D^{LSGAN} = -\mathbb{E}</em>{x \sim p_d}[(D(x) - 1)^2] + \mathbb{E}_{\hat{x} \sim p_g}[D(\hat{x})^2] )</td>
<td>( \mathcal{L}<em>G^{LSGAN} = -\mathbb{E}</em>{\hat{x} \sim p_g}[(D(\hat{x} - 1)^2] )</td>
</tr>
<tr>
<td>DRAGAN</td>
<td>( \mathcal{L}_D^{DRAGAN} = \mathcal{L}<em>D^{GAN} + \lambda \mathbb{E}</em>{\hat{x} \sim p_d + N(0,c)}[(</td>
<td></td>
</tr>
<tr>
<td>BEGAN</td>
<td>( \mathcal{L}<em>D^{BEGAN} = \mathbb{E}</em>{x \sim p_d}[</td>
<td></td>
</tr>
</tbody>
</table>

[Lucic, Kurach et al. (2018): Are GANs Created Equal? A Large-Scale Study]
Simultaneously training G/D?

\[ J^{(G)} = -\frac{1}{m_g} \sum_{i=1}^{m_g} \log(D(G(z^{(i)}))) \]

Non-saturating cost

\[ J^{(G)} = \frac{1}{m_g} \sum_{i=1}^{m_g} \log(1 - D(G(z^{(i)}))) \]

Saturating cost

for num_iterations:

for k iterations:

update D

update G

[Ian Goodfellow (2014): NIPS Tutorial: GANs]
Recap: GANs’ training tips

- Modification of the cost function
- Keep D up-to-date with respect to G (k update for D / 1 update for G)

And a lot more, GANs are hard to train!

[Soumith et al. (2016): GanHacks]
[Lucic, Kurach et al. (2018): Are GANs Created Equal? A Large-Scale Study]
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E. In terms of code

[Ian J. Goodfellow, Jonathon Shlens & Christian Szegedy (2015): Explaining and harnessing adversarial examples]
II.E - Nice results

Operation on codes

{\begin{array}{c}
\text{Code 1} \\
\begin{pmatrix}
0.12 \\
\vdots \\
0.92 \\
\end{pmatrix}
\end{array}} \xrightarrow{\text{Generator “G” (Neural Network)}} \begin{array}{c}
\text{(64,64,3) generated image}
\end{array}

{\begin{array}{c}
\text{Code 2} \\
\begin{pmatrix}
0.47 \\
\vdots \\
0.19 \\
\end{pmatrix}
\end{array}} \xrightarrow{\text{Generator “G” (Neural Network)}} \begin{array}{c}
\text{(64,64,3) generated image}
\end{array}

{\begin{array}{c}
\text{Code 3} \\
\begin{pmatrix}
0.42 \\
\vdots \\
0.07 \\
\end{pmatrix}
\end{array}} \xrightarrow{\text{Generator “G” (Neural Network)}} \begin{array}{c}
\text{(64,64,3) generated image}
\end{array}

\begin{array}{c}
\begin{pmatrix}
0.12 \\
\vdots \\
0.92 \\
\end{pmatrix} - \begin{pmatrix}
0.47 \\
\vdots \\
0.19 \\
\end{pmatrix} + \begin{pmatrix}
0.42 \\
\vdots \\
0.07 \\
\end{pmatrix}
\end{array} \xrightarrow{\text{Generator “G” (Neural Network)}} \begin{array}{c}
\text{(64,64,3) generated image}
\end{array}

\text{Man with glasses - man + woman = woman with glasses}

[Radford et al. (2015): UNSUPERVISED REPRESENTATION LEARNING WITH DEEP CONVOLUTIONAL GENERATIVE ADVERSARIAL NETWORKS]
II.E - Nice results

**Face Generation:**

[Karras et al. (2018): A Style-Based Generator Architecture for Generative Adversarial Networks]

https://www.youtube.com/watch?v=kSLJriaOumA&feature=youtu.be
II.E - Nice results

Image Generation:

Samples from the “generated distribution”

[Zhang et al. (2017): StackGAN++]
Figure 3: Street scene image translation results. For each pair, left is input and right is the translated image.
II.E - Nice results

[Zhu, Park et al. (2017): Unpaired Image-to-Image Translation using Cycle-Consistent Adversarial Networks]
<table>
<thead>
<tr>
<th>Data?</th>
<th>Architecture?</th>
<th>Cost?</th>
</tr>
</thead>
<tbody>
<tr>
<td>Unpaired images</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Horse images</td>
<td>Zebra images</td>
<td></td>
</tr>
</tbody>
</table>

**Goal:** Convert horses to zebras on images, and vice-versa.

[Zhu, Park et al. (2017): Unpaired Image-to-Image Translation using Cycle-Consistent Adversarial Networks]

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II.E - Nice results

Architecture?

\[ y = \begin{cases} 
0 & \text{if } x = G_2(Z) \\
1 & \text{otherwise } (x = h)
\end{cases} \]

\[ y = \begin{cases} 
0 & \text{if } x = G_1(H) \\
1 & \text{otherwise } (x = z)
\end{cases} \]

[Zhu, Park et al. (2017): Unpaired Image-to-Image Translation using Cycle-Consistent Adversarial Networks]
II.E - Nice results

Loss to minimize?

\[ J^{(D1)} = -\frac{1}{m_{\text{real}}} \sum_{i=1}^{m_{\text{real}}} \log(D1(z^{(i)})) - \frac{1}{m_{\text{gen}}} \sum_{i=1}^{m_{\text{gen}}} \log(1 - D1(G1(H^{(i)}))) \]

\[ J^{(G1)} = -\frac{1}{m_{\text{gen}}} \sum_{i=1}^{m_{\text{gen}}} \log(D1(G1(H^{(i)}))) \]

\[ J^{(D2)} = -\frac{1}{m_{\text{real}}} \sum_{i=1}^{m_{\text{real}}} \log(D2(h^{(i)})) - \frac{1}{m_{\text{gen}}} \sum_{i=1}^{m_{\text{gen}}} \log(1 - D2(G2(Z^{(i)}))) \]

\[ J^{(G2)} = -\frac{1}{m_{\text{gen}}} \sum_{i=1}^{m_{\text{gen}}} \log(D2(G2(Z^{(i)}))) \]

\[ J_{\text{cycle}} = \frac{1}{m_{\text{gen}}} \sum_{i=1}^{m_{\text{gen}}} \| G2(G1(H^{(i)})) - H^{(i)} \|_1 + \frac{1}{m_{\text{gen}}} \sum_{i=1}^{m_{\text{gen}}} \| G1(G2(Z^{(i)})) - Z^{(i)} \|_1 \]

\[ J = J^{(D1)} + J^{(G1)} + J^{(D2)} + J^{(G2)} + \lambda J_{\text{cycle}} \]

Kian Katanforoosh
CycleGANs:

Face2Ramen

+ Face detection

[Shu Naritomi et al.: Face2Ramen]
[Takuya Tako: Face2Ramen using CycleGAN]
[Zhu, Park et al. (2017): Unpaired Image-to-Image Translation using Cycle-Consistent Adversarial Networks]
II.E - Nice results

Pix2Pix:

https://affinelayer.com/pixsrv/ by Christopher Hesse.

[Isola et al. (2017): Image-to-Image Translation with Conditional Adversarial Networks]
II.E - Nice results

Super-resolution

Human Portrait Super Resolution Using GANs

Yujie Shu

Figure 1: Input LR 32x32, SRPGGAN 8x Output 256x256, and Original HR 256x256

II.E - Nice results

Motion Retargeting video subjects: https://www.youtube.com/watch?
Other applications of GANs:

- Beaulieu-Jones et al., Privacy-preserving generative deep neural networks support clinical data sharing.
- Hwang et al., Learning Beyond Human Expertise with Generative Models for Dental Restorations.
- Gomez et al., Unsupervised cipher cracking using discrete GANs.
- Many more…
For Tuesday 04/29, 9am:

C2M1
• Quiz: Practical aspects of deep learning
• Programming assignment: Initialization
• Programming assignment: Regularization
• Programming assignment: Gradient Checking

C2M2
• Quiz: Optimization Algorithms
• Programming assignment: Optimization

Project Proposal due on Wednesday 04/22 11:59pm PT. You also have until that time to meet with a TA regarding your project.

This Friday 04/24: TA section
II. Generative Adversarial Networks (GANs)

A. Motivation

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D. Nice results

E. In terms of code

[Ian J. Goodfellow, Jonathon Shlens & Christian Szegedy (2015): Explaining and harnessing adversarial examples]
II. D. In terms of code

```python
# Build and compile the discriminator
self.discriminator = self.build_discriminator()
self.discriminator.compile(loss='binary_crossentropy', optimizer=optimizer,
                         metrics=['accuracy'])

# Build the generator
self.generator = self.build_generator()

# The generator takes noise as input and generates imgs
z = Input(shape=(self.latent_dim,))
img = self.generator(z)

# For the combined model we will only train the generator
self.discriminator.trainable = False

# The discriminator takes generated images as input and determines validity
validity = self.discriminator(img)

# The combined model (stacked generator and discriminator)
# Trains the generator to fool the discriminator
self.combined = Model(z, validity)
self.combined.compile(loss='binary_crossentropy', optimizer=optimizer
```
# Build and compile the discriminator
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self.combined = Model(z, validity)
self.combined.compile(loss='binary_crossentropy', optimizer=optimizer)

def build_generator(self):
    model = Sequential()
    model.add(Dense(256, input_dim=self.latent_dim))
    model.add(LeakyReLU(alpha=0.2))
    model.add(BatchNormalization(momentum=0.8))
    model.add(Dense(512))
    model.add(LeakyReLU(alpha=0.2))
    model.add(BatchNormalization(momentum=0.8))
    model.add(Dense(1024))
    model.add(LeakyReLU(alpha=0.2))
    model.add(BatchNormalization(momentum=0.8))
    model.add(Dense(np.prod(self.img_shape), activation='tanh'))
    model.add(Reshape(self.img_shape))
    model.summary()

    noise = Input(shape=(self.latent_dim,))
    img = model(noise)
    return Model(noise, img)
II. D. In terms of code

```python
for epoch in range(epochs):
    # ---------------------
    # Train Discriminator
    # ---------------------

    # Select a random batch of images
    idx = np.random.randint(0, X_train.shape[0], batch_size)
    imgs = X_train[idx]
    noise = np.random.normal(0, 1, (batch_size, self.latent_dim))

    # Generate a batch of new images
    gen_imgs = self.generator.predict(noise)

    # Train the discriminator
    d_loss_real = self.discriminator.train_on_batch(imgs, valid)
    d_loss_fake = self.discriminator.train_on_batch(gen_imgs, fake)
    d_loss = 0.5 * np.add(d_loss_real, d_loss_fake)

    # ---------------------
    # Train Generator
    # ---------------------

    noise = np.random.normal(0, 1, (batch_size, self.latent_dim))

    # Train the generator (to have the discriminator label samples as valid)
    g_loss = self.combined.train_on_batch(noise, valid)
```

[Link to GitHub repository]