

Probabilistic and Multimodal Trajectory Predictions for Autonomous Driving

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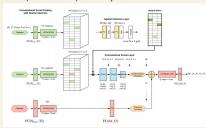
1. Abstract

- We study the problem of Trajectory Predictions for Autonomous Driving
- We investigate different architectures: RNN-LSTM variants and Transformer applicability to trajectory predictions
- We propose enhancements with Spatial Attention in addition to Convolutional Social pooling
- We improve results over a state-of-the-art baseline [2]

3. Methods

3.1 Convolutional Social pooling enhanced with Spatial Attention: CSSA-LSTM(M)

We enhance CS-LSTM(M) [2]: like a human driver we do not focus equally on every neighbors and we learn the best attention weights depending on the spatio-temporal relationships of the objects and additional features related to behavior and shapes.



3.2 Loss Function

We predict a 2D trajectory with a multimodal and probabilistic model: at each time step, a 5D vector corresponding to the param eters of a bivariate Gaussian distribution is derived. For maneuver predictions we use cross-entropy loss functions.

$$\begin{split} \bullet & f\left(x,y\right) = \frac{1}{2\pi\sigma_{\chi}\sigma_{\gamma}\sqrt{1-\rho^{2}}} \exp\left(-\frac{1}{21-\rho^{2}}\left[\frac{(z-\mu_{z})^{2}}{\sigma_{\chi}^{2}} + \frac{(y-\mu_{z})^{2}}{\sigma_{\zeta}^{2}} - \frac{2\rho(z-\mu_{\chi})(y-\mu_{z})}{\sigma_{\chi}\sigma_{y}}\right]\right) \\ \bullet & \mu = \begin{bmatrix} \mu_{X} \\ \mu_{Y} \end{bmatrix}, \Sigma = \begin{bmatrix} \sigma_{X}^{2} & \rho\sigma_{\chi}\sigma_{Y} \\ \rho\sigma_{X}\sigma_{Y} & \sigma_{Y}^{2} \end{bmatrix} \text{ with -1$\!\! 2$} \rho \le 1, \sigma_{\chi} \geq 0, \sigma_{Y} \geq 0 \end{split}$$

$$\bullet \ L_{\mathrm{nii}}(\mathrm{targete} \begin{bmatrix} x \\ y \end{bmatrix}, \mathrm{predictede} \begin{bmatrix} \mu_X \\ \mu_Y \\ \sigma_X \\ \rho \end{bmatrix} \rightarrow \log \left(\sigma_X \sigma_Y \sqrt{1-\rho^2} \right) + \frac{1}{1-\rho^2} \left[\frac{(v-y_i)^2}{\sigma_X^2} + \frac{(v-y_i)^2}{\sigma_Y^2} - \frac{2\rho(v-y_X)(v-y_Y)}{\sigma_X \sigma_Y} \right] - \frac{1}{\rho^2} \left[\frac{(v-y_i)^2}{\sigma_X^2} + \frac{(v-y_i)^2}{\sigma_X^2} - \frac{2\rho(v-y_X)(v-y_Y)}{\sigma_X \sigma_Y} \right] - \frac{1}{\rho^2} \left[\frac{(v-y_i)^2}{\sigma_X^2} + \frac{(v-y_i)^2}{\sigma_X^2} - \frac{2\rho(v-y_X)(v-y_Y)}{\sigma_X \sigma_Y} \right] - \frac{1}{\rho^2} \left[\frac{(v-y_i)^2}{\sigma_X^2} + \frac{(v-y_i)^2}{\sigma_X^2} - \frac{2\rho(v-y_X)(v-y_Y)}{\sigma_X^2} \right] - \frac{1}{\rho^2} \left[\frac{(v-y_i)^2}{\sigma_X^2} + \frac{(v-y_i)^2}{\sigma_X^2} - \frac{2\rho(v-y_X)(v-y_Y)}{\sigma_X^2} \right] - \frac{1}{\rho^2} \left[\frac{(v-y_i)^2}{\sigma_X^2} + \frac{(v-y_i)^2}{\sigma_X^2} - \frac{2\rho(v-y_i)^2}{\sigma_X^2} \right] - \frac{1}{\rho^2} \left[\frac{(v-y_i)^2}{\sigma_X^2} + \frac{(v-y_i)^2}{\sigma_X^2} - \frac{2\rho(v-y_i)^2}{\sigma_X^2} \right] - \frac{1}{\rho^2} \left[\frac{(v-y_i)^2}{\sigma_X^2} + \frac{(v-y_i)^2}{\sigma_X^2} - \frac{2\rho(v-y_i)^2}{\sigma_X^2} \right] - \frac{1}{\rho^2} \left[\frac{(v-y_i)^2}{\sigma_X^2} + \frac{(v-y_i)^2}{\sigma_X^2} - \frac{2\rho(v-y_i)^2}{\sigma_X^2} \right] - \frac{1}{\rho^2} \left[\frac{(v-y_i)^2}{\sigma_X^2} + \frac{(v-y_i)^2}{\sigma_X^2} - \frac{2\rho(v-y_i)^2}{\sigma_X^2} \right] - \frac{1}{\rho^2} \left[\frac{(v-y_i)^2}{\sigma_X^2} + \frac{(v-y_i)^2}{\sigma_X^2} - \frac{2\rho(v-y_i)^2}{\sigma_X^2} \right] - \frac{1}{\rho^2} \left[\frac{(v-y_i)^2}{\sigma_X^2} + \frac{(v-y_i)^2}{\sigma_X^2} - \frac{2\rho(v-y_i)^2}{\sigma_X^2} \right] - \frac{1}{\rho^2} \left[\frac{(v-y_i)^2}{\sigma_X^2} + \frac{(v-y_i)^2}{\sigma_X^2} - \frac{(v-y_i)^2}{\sigma_X^2} \right] - \frac{1}{\rho^2} \left[\frac{(v-y_i)^2}{\sigma_X^2} + \frac{(v-y_i)^2}{\sigma_X^2} - \frac{(v-y_i)^2}{\sigma_X^2} \right] - \frac{1}{\rho^2} \left[\frac{(v-y_i)^2}{\sigma_X^2} + \frac{(v-y_i)^2}{\sigma_X^2} - \frac{(v-y_i)^2}{\sigma_X^2} \right] - \frac{(v-y_i)^2}{\sigma_X^2} - \frac{(v-y_i)^2}{\sigma$$

 $\mathsf{Loss} = L_{\mathsf{nll}} + L_{\mathsf{Crossent-lateral}} + L_{\mathsf{Crossent-longitudinal}}$

5. Conclusions and Future Work

- We investigated how to apply Transfomer models to trajectory predictions
- We enhanced Convolutional Social pooling with Spatial Attention
- We improved results over a state-of-the-art baseline [2] by 10%
- Future work; experiment in heterogeneous urban environments where Spatial Attention should be even more relevant

2. Dataset and Features

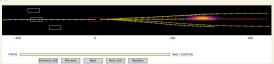
- NGSIM US Highway 101 dataset (US-101) and Interstate 80 Freeway dataset (I-80)
- The datasets of 90 minutes recording is captured from a bird's-eye view of the highway with a static camera at 10 Hz
- 8.3 millions samples split into 70,10,20 % for the training, development and test set, as used in [2]
- $\bullet \ \ \text{We use only legacy and raw NGSIM features: } (x,y,Vel,Accel,Class). \ \ \text{Additional Behavioral features were not experimented }$

4. Experiments and Results

4.1 Experiments

- Teacher forcing results in overfitting for all models; Batch size should be increased as much as possible for Transformer [4]
- For Transformer [3]: with a smaller dataset, we tend to overfit even with dropouts. Finally we use a smaller model with $N_{layers} = 1, d_{model} = 256, d_{feed-forward} = 256, h_{heads} = 4; \\ \textbf{lots of proposed optimizations and tricks in [3] are NLP specifical properties of the proposed optimization of the properties of the$
- Seq2seq is 10 times smaller, faster to train (per epoch) and to converge (fewer epochs) than Transformer for similar accuracy
- RNN-LSTM: using a seq2seq architecture, a bidirectional encoder, additional layers, increasing the decoder size and varying the default settings of CS-LSTM(M) does not improve over the baseline [2]
- Spatial attention capturing weighted interactions is more useful than temporal attention (weighting only grids and not grid cells)

4.2 Visualization



The bivariate gaussian is visualized for most probable maneuver at a time horizon of 3 seconds: $\sigma_{longitudinal} \gg \sigma_{lateral}$

4.3 RMSE Results on NGSIM dataset

| Time (sec) | CV | Deo and Trivedi [2] | Seq2seq | Transformer | CSSA-LSTM(M) |
|------------|------|---------------------|---------|-------------|--------------|
| 1 | 0.73 | 0.58 | 0.59 | 0.52 | 0.42 |
| 2 | 1.78 | 1.27 | 1.28 | 1.23 | 1.06 |
| 3 | 3.13 | 2.12 | 2.14 | 2.17 | 1.85 |
| 4 | 4.78 | 3.19 | 3.25 | 3.23 | 2.85 |
| 5 | 6.68 | 4.51 | 4.59 | 4.70 | 4.11 |

We improve by enabling additional features processing capabilities with Spatial Attention on top of the Convolutional Social layer

6. References

- [1] Ernest Cheung. Identifying driver behaviors using trajectory features for vehicle navigation. 2018. [2] N. Deo and M.M. Trivedi. Convolutional social pooling for vehicle trajectory prediction. CVPR, 2018.
- [3] Lukasz Kaiser et al. Attention is all you need. NIPS, 2017.
- [4] Martin Popel and Ondrej Bojar. Training tips for the transformer model. 2018.

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