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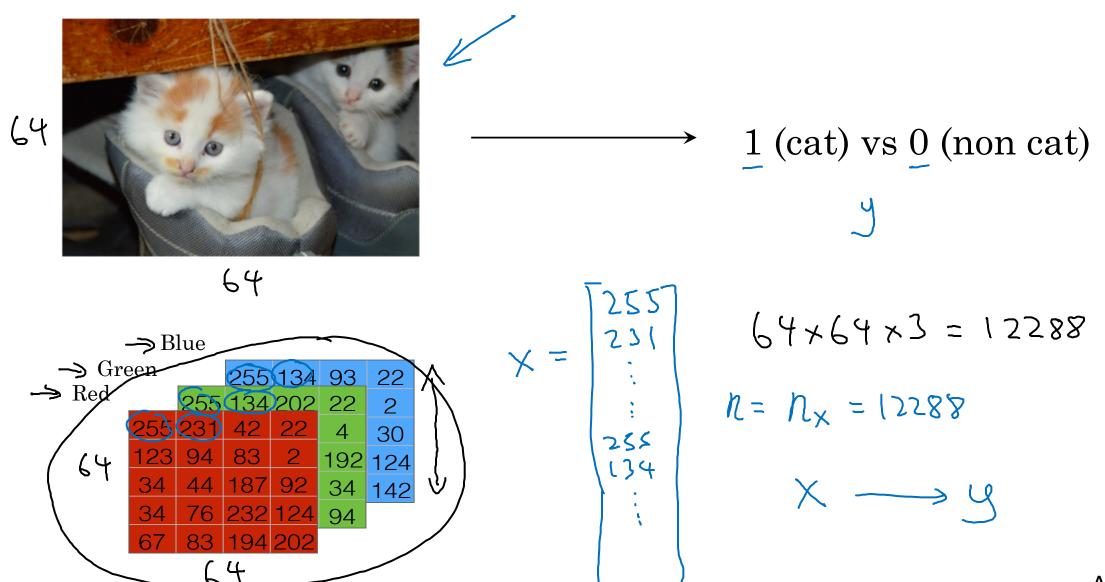
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Basics of Neural Network Programming

Binary Classification

Binary Classification



Andrew Ng

Notation

$$(x,y)$$
 $\times \in \mathbb{R}^{n_x}$, $y \in \{0,1\}$
 $m \leftarrow \text{trainiy}$ examples: $\{(x^{(i)},y^{(i)}),(x^{(i)},y^{(2i)}),...,(x^{(m)},y^{(m)})\}$
 $M = M \leftarrow \text{train}$ $M \leftarrow \text{test} = \text{thest}$ examples.
 $X = \begin{bmatrix} x^{(i)} & x^{(2i)} & \dots & x^{(m)} \end{bmatrix}$
 $X = \begin{bmatrix} x^{(i)} & x^{(2i)} & \dots & x^{(m)} \end{bmatrix}$
 $X \in \mathbb{R}^{n_x \times m}$ $X \in \mathbb{R}^{n_x \times m}$
 $X \in \mathbb{R}^{n_x \times m}$ $X \in \mathbb{R}^{n_x \times m}$



Basics of Neural Network Programming

Logistic Regression

Logistic Regression

Given
$$x$$
, want $y = P(y=1|x)$
 $x \in \mathbb{R}^{n}x$
Parareters: $w \in \mathbb{R}^{n}x$, $b \in \mathbb{R}$.
Output $y = \sigma(w^{T}x + b)$
Output $y = \sigma(x)$

$$X_0 = 1, \quad x \in \mathbb{R}^{n_x + 1}$$

$$\hat{y} = 6 (0^{T}x)$$

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Basics of Neural Network Programming

Logistic Regression cost function

Logistic Regression cost function

Given
$$\{(x^{(1)}, y^{(1)}), \dots, (x^{(m)}, y^{(m)})\}$$
, want $\hat{y}^{(i)} \approx y^{(i)}$.

Since $\{(x^{(1)}, y^{(1)}), \dots, (x^{(m)}, y^{(m)})\}$, want $\hat{y}^{(i)} \approx y^{(i)}$.

Loss (error) function: $\int_{\mathcal{C}} (\hat{y}, y) = \frac{1}{2} (\hat{y} - y)^2$

The entropy of the second of the



Basics of Neural Network Programming

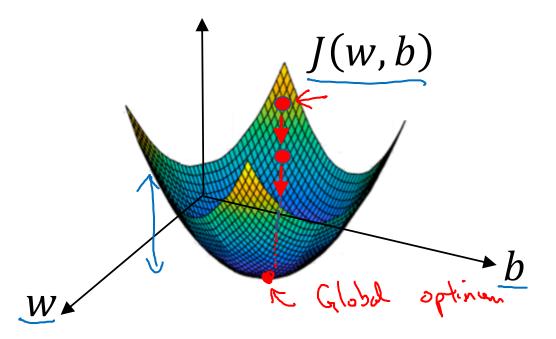
Gradient Descent

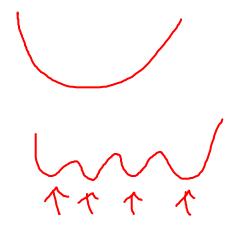
Gradient Descent

Recap:
$$\hat{y} = \sigma(w^T x + b)$$
, $\sigma(z) = \frac{1}{1 + e^{-z}}$

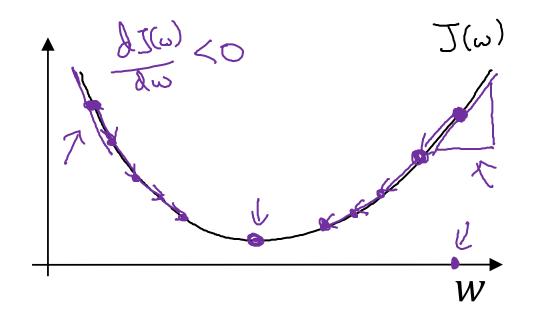
$$\underline{J(w,b)} = \frac{1}{m} \sum_{i=1}^{m} \mathcal{L}(\hat{y}^{(i)}, y^{(i)}) = -\frac{1}{m} \sum_{i=1}^{m} y^{(i)} \log \hat{y}^{(i)} + (1 - y^{(i)}) \log(1 - \hat{y}^{(i)})$$

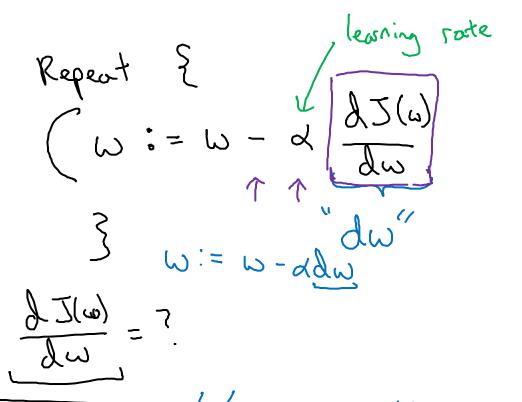
Want to find w, b that minimize I(w, b)





Gradient Descent





$$J(\omega,b)$$

$$b:=b-\lambda \frac{\partial J(\omega,b)}{\partial \omega}$$

$$\frac{\partial J(\omega,b)}{\partial \omega}$$

$$\frac{\partial J(\omega,b)}{\partial \omega}$$

$$\frac{\partial J(\omega,b)}{\partial \omega}$$

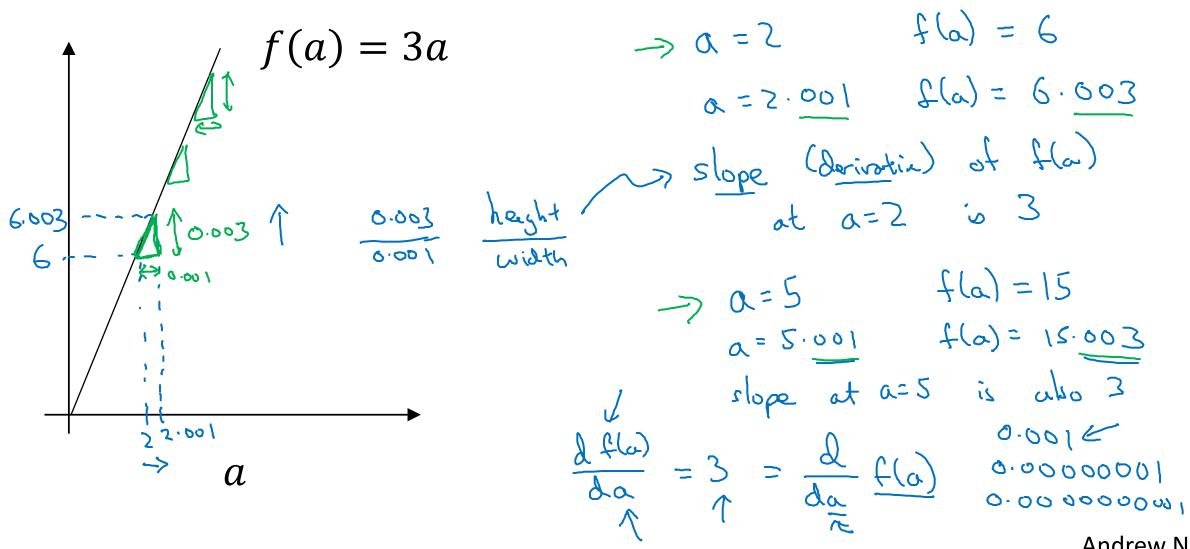
Andrew Ng



Basics of Neural Network Programming

Derivatives

Intuition about derivatives



Andrew Ng

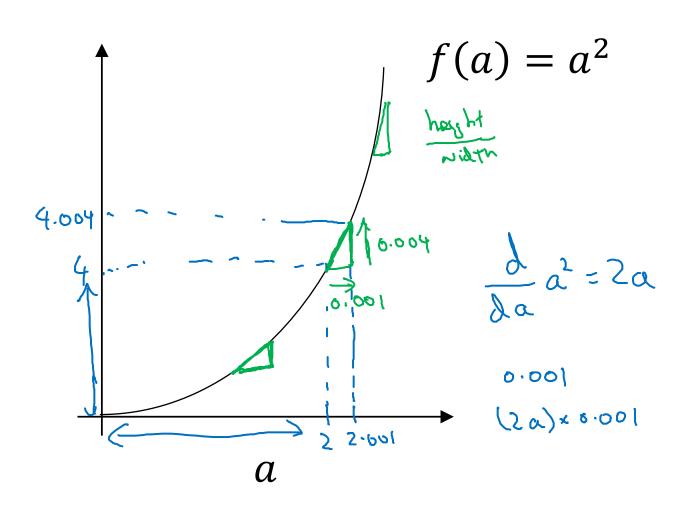


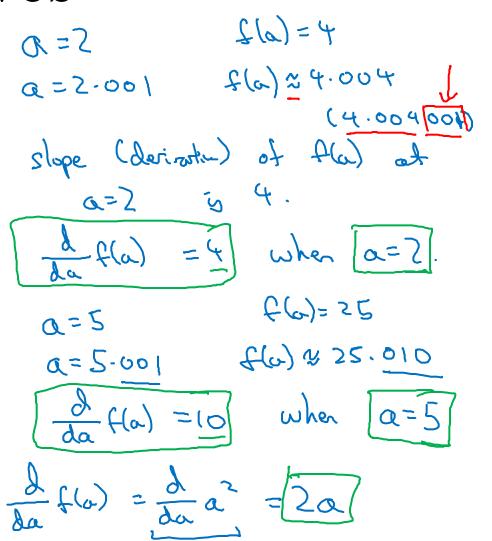
Basics of Neural Network Programming

More derivatives examples

Intuition about derivatives







More derivative examples

$$f(a) = a^2$$

$$f(\omega) = \alpha^3$$

$$\frac{d}{da}(a) = 3a^{2}$$
 $3x2^{3} = 12$

$$a = 2$$
 $f(a) = 4$
 $a = 2-001$ $f(a) = 4-004$

$$a = 5.001$$
 $f(a) = 8$
 $a = 5.001$ $f(a) = 8$

$$0.0002 < 0.0002$$

$$0.0002 < 0.0002$$

$$0.0002 < 0.0002$$



Basics of Neural Network Programming

Computation Graph

Computation Graph

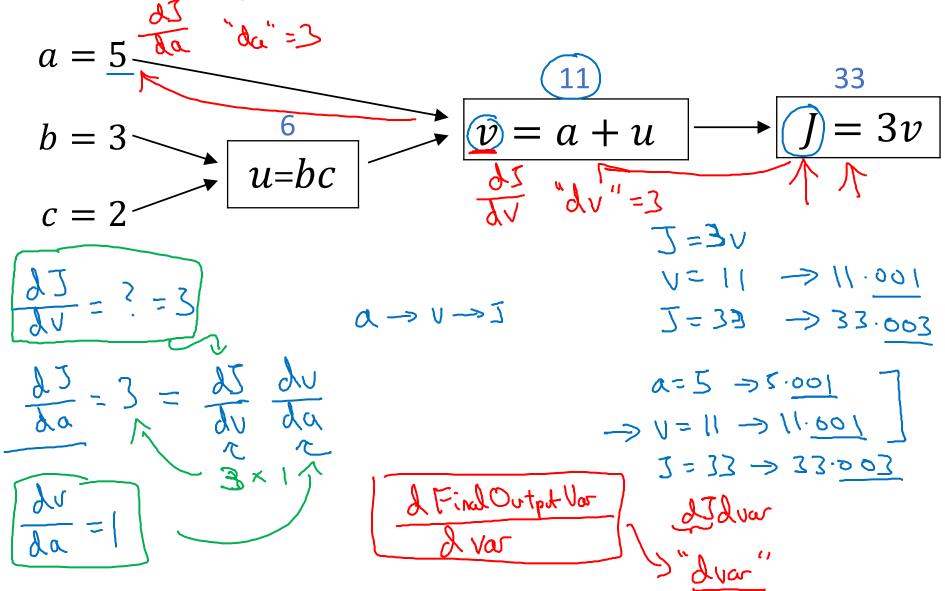
$$J(a,b,c) = 3(a+bc) = 3(5+3*2) = 33$$
 $U = bc$
 $V = a+u$
 $J = 3v$
 $U = bc$
 $U = bc$
 $U = bc$
 $U = a+u$
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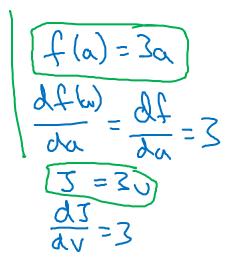


Basics of Neural Network Programming

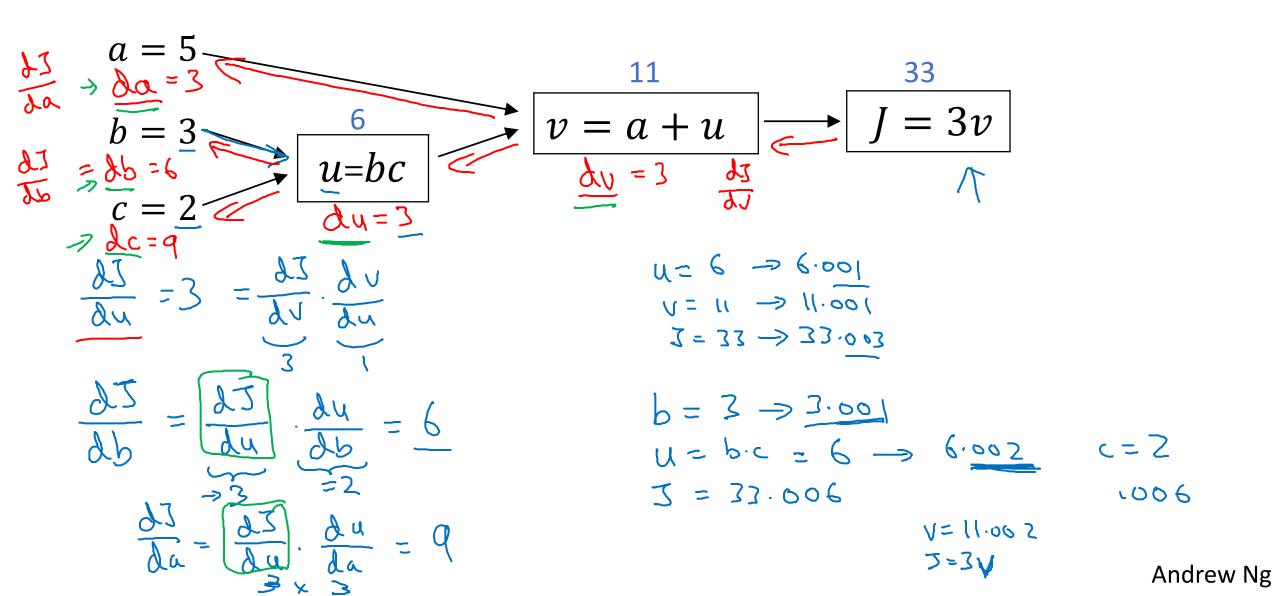
Derivatives with a Computation Graph

Computing derivatives





Computing derivatives





Basics of Neural Network Programming

Logistic Regression Gradient descent

Logistic regression recap

$$\Rightarrow z = w^{T}x + b$$

$$\Rightarrow \hat{y} = a = \sigma(z)$$

$$\Rightarrow \mathcal{L}(a, y) = -(y \log(a) + (1 - y) \log(1 - a))$$

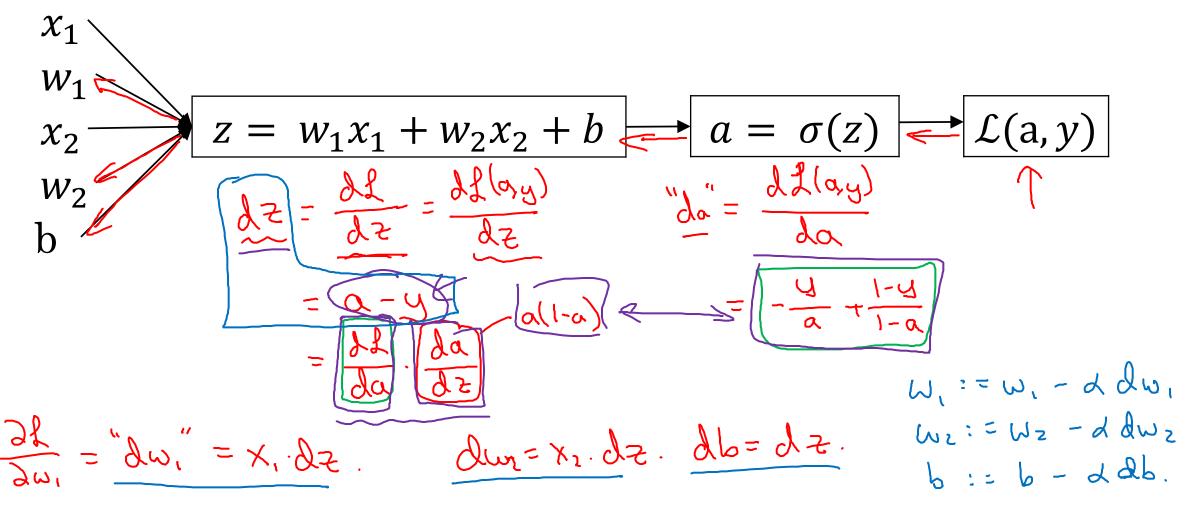
$$\begin{cases} \lambda_{1} \\ \lambda_{2} \\ \lambda_{3} \end{cases}$$

$$\begin{cases} \lambda_{1} \\ \lambda_{2} \\ \lambda_{3} \end{cases}$$

$$\begin{cases} \lambda_{2} \\ \lambda_{3} \end{cases}$$

$$\begin{cases} \lambda_{1} \\ \lambda_{2} \\ \lambda_{3} \end{cases}$$

Logistic regression derivatives





Basics of Neural Network Programming

Gradient descent on m examples

Logistic regression on m examples

$$\frac{J(u,b)}{J(u,b)} = \frac{1}{m} \sum_{i=1}^{m} f(a^{(i)}, y^{(i)}) \\
\Rightarrow a^{(i)} = f(x^{(i)}) = G(x^{(i)}, y^{(i)}) \\
\frac{\partial}{\partial u_i} J(u,b) = \frac{1}{m} \sum_{i=1}^{m} \frac{\partial}{\partial u_i} f(a^{(i)}, y^{(i)}) \\
\frac{\partial u_i}{\partial u_i} - (x^{(i)}, y^{(i)})$$

Logistic regression on m examples

$$J=0; dw_{1}=0; dw_{2}=0; db=0$$

$$Z^{(i)} = \omega^{T} x^{(i)} + b$$

$$Q^{(i)} = G(Z^{(i)})$$

$$J+=-[y^{(i)}(\log Q^{(i)} + (1-y^{(i)})\log(1-Q^{(i)})]$$

$$dZ^{(i)} = Q^{(i)} - y^{(i)}$$

$$dW_{1} + = X^{(i)} dZ^{(i)}$$

$$dw_{2} + = X^{(i)} dZ^{(i)}$$

$$dw_{2} + = X^{(i)} dZ^{(i)}$$

$$J = 0; dw_{2} + Q^{(i)}$$

$$dZ^{(i)} = Q^{(i)} - Q^{(i)}$$

$$dW_{2} + Z^{(i)} dZ^{(i)}$$

$$dW_{2} + Z^{(i)} dZ^{(i)}$$

$$dW_{3} + Z^{(i)} dZ^{(i)}$$

$$dW_{4} + Z^{(i)} dZ^{(i)}$$

$$dW_{5} + Z^{(i)} dZ^{(i)}$$

$$dW_{7} + Z^{(i)} dZ^{$$

$$d\omega_1 = \frac{\partial J}{\partial \omega_1}$$
 $\omega_1 := \omega_1 - d d\omega_1$
 $\omega_2 := \omega_2 - \alpha d\omega_2$
 $b := b - d db$

Vectorization



Basics of Neural Network Programming

Vectorization

What is vectorization?

for i in ray
$$(n-x)$$
:
 $2+=\omega [1] + x[1]$



Basics of Neural Network Programming

More vectorization examples

Neural network programming guideline

Whenever possible, avoid explicit for-loops.

$$U = AV$$

$$U_{i} = \sum_{i} \sum_{j} A_{ij} V_{j}$$

$$U = np.zeros((n, i))$$

$$for i \dots \subseteq ACIJCIJ * vC_{i}J$$

$$uCiJ += ACIJCIJ * vC_{i}J$$

Vectors and matrix valued functions

Say you need to apply the exponential operation on every element of a matrix/vector.

$$v = \begin{bmatrix} v_1 \\ \vdots \\ v_n \end{bmatrix} \rightarrow \mathbf{u} = \begin{bmatrix} \mathbf{e}^{\mathbf{v}_1} \\ \mathbf{e}^{\mathbf{v}_2} \end{bmatrix}$$

$$v = \begin{bmatrix} v_1 \\ \vdots \\ v_n \end{bmatrix} \rightarrow u = \begin{bmatrix} e^{v_1} \\ e^{v_n} \end{bmatrix}$$

$$u = \text{np. exp}(v) \leftarrow$$

$$\text{np. log}(v)$$

$$\text{np. abs}(v)$$

$$\text{np. havinum}(v, o)$$

Logistic regression derivatives

$$J = 0, \quad dw1 = 0, \quad dw2 = 0, \quad db = 0$$

$$\Rightarrow \text{ for } i = 1 \text{ to } n:$$

$$z^{(i)} = w^{T}x^{(i)} + b$$

$$a^{(i)} = \sigma(z^{(i)})$$

$$J + = -[y^{(i)}\log\hat{y}^{(i)} + (1 - y^{(i)})\log(1 - \hat{y}^{(i)})]$$

$$dz^{(i)} = a^{(i)}(1 - a^{(i)})$$

$$dw_{1} + x_{1}^{(i)}dz^{(i)}$$

$$dw_{2} + x_{2}^{(i)}dz^{(i)}$$

$$db + dz^{(i)}$$

$$J = J/m, \quad dw_{1} = dw_{1}/m, \quad dw_{2} = dw_{2}/m, \quad db = db/m$$

$$d\omega / = m$$



Basics of Neural Network Programming

Vectorizing Logistic Regression

Vectorizing Logistic Regression

$$Z^{(1)} = w^{T}x^{(1)} + b$$

$$Z^{(2)} = w^{T}x^{(2)} + b$$

$$Z^{(3)} = w^{T}x^{(3)} + b$$

$$Z^{(3)} = \sigma(z^{(3)})$$

$$Z^$$



Basics of Neural Network Programming

Vectorizing Logistic Regression's Gradient Computation

Vectorizing Logistic Regression

$$\frac{dz^{(1)} = a^{(1)} - y^{(1)}}{dz^{(2)}} = a^{(2)} - y^{(2)}$$

$$\frac{dz^{(1)} = a^{(1)} - y^{(1)}}{dz^{(2)}} = a^{(2)} - y^{(2)}$$

$$A = [a^{(1)} - a^{(1)}] \quad Y = [y^{(1)} - y^{(2)}]$$

$$A = [a^{(1)} - a^{(1)}] \quad Y = [y^{(1)} - y^{(2)}]$$

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$$A = [a^{(1)} - y^{(1)}] \quad a$$

$$db = \frac{1}{m} \sum_{i=1}^{n} dz^{(i)}$$

$$= \frac{1}{m} \left[x^{(i)} + \dots + x^{(n)} dz^{(m)} \right]$$

$$= \frac{1}{m} \left[x^{(i)} + \dots + x^{(n)} dz^{(m)} \right]$$

$$= \frac{1}{m} \left[x^{(i)} + \dots + x^{(n)} dz^{(m)} \right]$$

$$= \frac{1}{m} \left[x^{(i)} + \dots + x^{(n)} dz^{(m)} \right]$$

Implementing Logistic Regression

J = 0,
$$dw_1 = 0$$
, $dw_2 = 0$, $db = 0$

for i = 1 to m:

$$z^{(i)} = w^T x^{(i)} + b$$

$$a^{(i)} = \sigma(z^{(i)})$$

$$J += -[y^{(i)} \log a^{(i)} + (1 - y^{(i)}) \log(1 - a^{(i)})]$$

$$dz^{(i)} = a^{(i)} - y^{(i)}$$

$$dw_1 += x_1^{(i)} dz^{(i)}$$

$$dw_2 += x_2^{(i)} dz^{(i)}$$

$$dw_2 += dz^{(i)}$$

$$dw_1 += dz^{(i)}$$

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$$dw_1 += dz^{(i)}$$

$$dw_2 += dz^{(i)}$$

$$dw_2 += dz^{(i)}$$

$$dw_3 += dz^{(i)}$$

$$dw_4 += dz^{(i)}$$

$$dw_5 += dz^{(i)}$$

$$dw_6 += dz^{(i)}$$

$$dw_6 += dz^{(i)}$$

$$dw_6 += dz^{(i)}$$

iter in range (1000):
$$C$$

$$Z = \omega^{T} X + b$$

$$= n p \cdot dot (\omega \cdot T \cdot X) + b$$

$$A = c (Z)$$

$$dZ = A - Y$$

$$dw = m \times dZ^{T}$$

$$db = m n p \cdot sun(dZ)$$

$$\omega := \omega - x d\omega$$

$$b := b - x d\omega$$



Basics of Neural Network Programming

Broadcasting in Python

Broadcasting example

Calories from Carbs, Proteins, Fats in 100g of different foods:

Apples Beef Eggs Potatoes

Carb
$$56.0$$
 0.0 4.4 68.0

Protein 1.2 104.0 52.0 8.0

Fat 1.8 135.0 99.0 0.9 (3,4)

Squal 56.0 99.0 0.9 (3,4)

Columbs of Glors from Carb, Poten, Fort. Can you do the arphint for-loop?

Cal = A.sum(axis = 0)

percentage = $100*A/(cal Abstrace(1.6))$

Broadcasting example

$$\begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \end{bmatrix} + \begin{bmatrix} 100 & 100 & 100 \\ 200 & 200 & 200 \end{bmatrix} = \begin{pmatrix} m_{1} & 1 \\ m_{2} & m_{3} \end{pmatrix}$$

General Principle

$$(m, n) \qquad + \qquad (n, n) \qquad motion \qquad + \qquad (m, n) \qquad modeling \qquad + \qquad (m, n) \qquad modeling \qquad + \qquad (m, n) \qquad + \qquad R \qquad + \qquad (m, n) \qquad + \qquad (m,$$

Mathab/Octave: bsxfun



Basics of Neural Network Programming

Explanation of logistic regression cost function (Optional)

Logistic regression cost function

Logistic regression cost function

If
$$y = 1$$
: $p(y|x) = \hat{y}$

If $y = 0$: $p(y|x) = 1 - \hat{y}$

$$p(y|x) = \hat{y} \cdot (1 - \hat{y})$$

Cost on *m* examples

log
$$p(lolods)$$
 in troops set) = log $\prod_{i=1}^{m} p(y(i)|\chi(i))$

log $p(----) = \sum_{i=1}^{m} log p(y(i)|\chi(i))$

Movimum likelihood setiment

$$- \chi(y(i), y(i))$$

$$= -\sum_{i=1}^{m} \chi(y(i), y(i))$$

(ost: $J(w, b) = \frac{1}{m} \sum_{i=1}^{m} \chi(y(i), y(i))$

(minimize)